

AD-A285 480



LEAKY WAVE RADIATION FROM A PERIODICALLY  
SLOTTED WAVEGUIDE

by

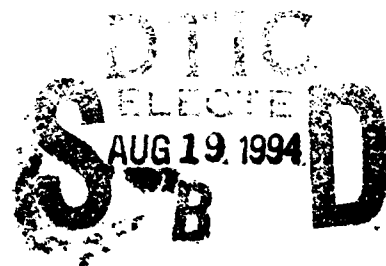
Jean-Paul Renault

Research Report PIBMRI-1151-63  
for

Air Force Cambridge Research Laboratories  
Office of Aerospace Research  
United States Air Force  
Bedford, Mass.

Contract No. AF-19(604)-7499  
Project 4600, Task 460004

May 8, 1963



DTIC QUALITY INSPECTED 5

94-24355



3385

MRI

94 8 02 012

POLYTECHNIC INSTITUTE OF BROOKLYN

MICROWAVE RESEARCH INSTITUTE  
ELECTROPHYSICS DEPARTMENT

"Requests for additional copies by Agencies of the Department of Defense, their contractors, and other Government Agencies should be directed to the:

DEFENSE DOCUMENTATION CENTER (DDC)  
Cameron Station  
Alexandria, Virginia

Department of Defense contractors must be established for DDC services or have their 'need-to-know' certified by the cognizant military agency of their project or contract. "

"All other persons and organizations should apply to the:

U.S. DEPARTMENT OF COMMERCE  
OFFICE OF TECHNICAL SERVICES  
WASHINGTON 25, D.C. "

Accession For		<input checked="checked" type="checkbox"/>
NTIS GRA&I		<input type="checkbox"/>
DTIC TAB		<input type="checkbox"/>
Unannounced		
Justification		
By _____		
Distribution/		
Availability Codes		
Dist	Avail and/or	Special
A-1		

LEAKY WAVE RADIATION FROM A PERIODICALLY  
SLOTTED WAVEGUIDE

by

Jean-Paul Renault

Polytechnic Institute of Brooklyn  
Microwave Research Institute  
55 Johnson Street  
Brooklyn 1, New York

Research Report PIBMRI-1151-63  
Contract No. AF-19(604)-7499

Project 4600

Task 460004

May 8, 1963

Title Page  
Acknowledgment  
Abstract  
Table of Contents  
16 pages of text  
Distribution

Jean-Paul Renault  
Jean-Paul Renault  
Research Fellow

Approved by:

H. J. Carlin

Head, Electrophysics Dept.

for

Air Force Cambridge Research Laboratories  
Office of Aerospace Research  
United States Air Force  
Bedford, Mass.

### ACKNOWLEDGMENT

The author is pleased to acknowledge the generous assistance of his late advisor, Prof. L. O. Goldstone, who first suggested many of the ideas used in this report.

The work reported herein was sponsored by the Air Force Cambridge Research Laboratories, Office of Aerospace Research, United States Air Force, Bedford, Massachusetts, under Contract No. AF-19(604)-7499.

## ABSTRACT

A rectangular waveguide with transverse slots located periodically in the broad wall is analysed by the transverse resonance procedure. The slots are replaced by equivalent conductances and susceptances; these are used in the resonance equation to obtain leaky and surface wave solutions.

The theoretical solutions for the complex axial propagation constant are found, and these results are verified experimentally. The transverse resonance method of solution is shown to present advantages over previously derived results.

## TABLE OF CONTENTS

- I. INTRODUCTION
  - (a) Methods of analysis of leaky wave structures
  - (b) Description of the problem
- II. ANALYSIS OF THE STRUCTURE
  - (a) Network representation
  - (b) Transverse resonance
    - 1. Leaky wave solution
    - 2. Surface wave solution
- III. RESULTS
  - (a) Theoretical
  - (b) Experimental
    - 1. Amplitude measurements
    - 2. Phase measurements
- IV. CONCLUSION

## I. INTRODUCTION

Leaky waves in many cases of practical interest are excited in lossless waveguides in which are cut either uniform or periodic apertures. These waves, which have a complex propagation constant, propagate along the leaky structure with a velocity greater than that of light and are continuously attenuated, indicating the leakage of energy they undergo as they travel. The theoretical discussion of leaky wave structures using only field considerations would, therefore, generally be extremely arduous, including particularly the solution of a discontinuity problem. But leaky waves are solutions of the source-free field equations, so their propagation constants can be calculated rigorously by means of a transverse resonance procedure. This procedure includes two steps: first it is necessary to find a transverse network representation, and then a resonance equation has to be solved. The first step consists mostly of evaluating the discontinuities. Generally, however, this does not need to be carried out since the results are already available in the literature. The next step consists of the solution of a network problem. The resonance equation is a complex transcendental equation which requires the use either of a computing machine or of numerical methods. However, when the solution can be regarded as a perturbation of the propagation constant of the closed waveguide, a perturbation technique may be used which leads to solutions in closed form where the functional behavior is immediately evident.

The theory of this network approach has already been discussed <sup>(1)</sup> and the evaluation of discontinuities has been carried out in many cases of practical interest <sup>(2)</sup>. In this report a transverse resonance procedure will be applied to a transversely-slotted rectangular waveguide as illustrated in Figure 1.

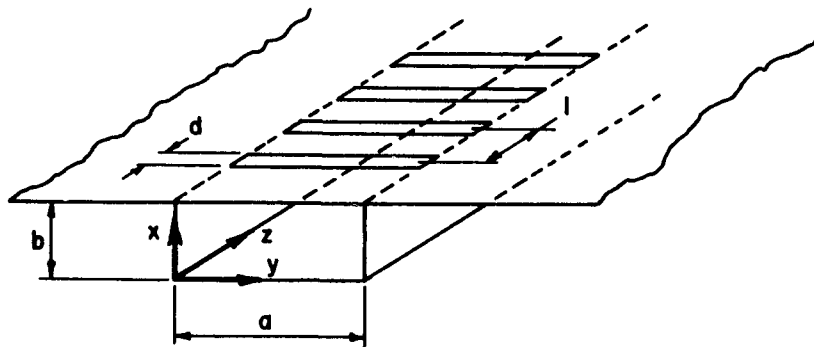


Figure 1. Transversely-slotted waveguide

- 
- (1) L. O. Goldstone and A. A. Oliner, "Leaky-wave Antennas I: Rectangular Waveguides," Research Report R-606-57, PIB 534 M. R. I.; August 57
- (2) N. Marcuvitz, "Waveguide Handbook", Rad. Lab. Series, Vol. 10, McGraw-Hill Book Co., New York, 1951

The structure consists of an array of closely-spaced transverse slots which extend completely across the broad face of a rectangular waveguide. The waveguide is assumed to be infinite, and its slotted face is inserted in an infinite conducting plane. This structure is well known and has already been studied by R. F. Hyneman<sup>(3)</sup>. However, it will be discussed here from a completely different point of view. Whereas Hyneman started from the general field equations and used iterative techniques with computing machines to get numerical results, in the following analysis a simple perturbation technique will be used to obtain simple closed form expressions for the guide wavelength and attenuation constant.

Experimental measurements have also been made of the attenuation constant and guide wavelength, and these measured results are compared with the theoretical expressions. It is found that very good agreement is obtained with the presently-derived theory, but that the calculations of Hyneman differ considerably from the measured values. Furthermore, Hyneman indicates that a surface wave is present on this structure, but the present theory finds no evidence of the presence of such a wave. These points are considered in detail below.

---

(3) R. F. Hyneman, "Closely-Spaced Transverse Slots in Rectangular Waveguide" IRE Transactions on Antennas and Propagation, Nb 4, pp. 335-342, October 1959.

## II. ANALYSIS OF THE STRUCTURE

A few restrictions have to be made in order to simplify the analysis of the problem. First, if the propagation constant of the leaky wave is to be regarded as a perturbation on the closed waveguide propagation constants, the slots have to be small, i. e., the ratio of length to width  $a/d$  must be sufficiently great, the ratio of width to free space wavelength  $d/\lambda$  sufficiently small, and the spacing of the slots must be large compared to their width. Under these conditions the only appreciable component of the tangential electric field in the apertures is the  $z$  component and the characteristics of the wave traveling on the structure are only slightly different from those of the unperturbed case and are thus susceptible to analysis by perturbation methods.

Then, if this structure is to exhibit a leaky-wave behavior, the leakage of energy has to be uniform. In other words, the structure has to be regarded as radiating continuously and not as a discrete array of apertures. This will be the case if the slots spacing is very small with respect to the free-space wavelength ( $l < \lambda$ ).

### (a) Network Representation

A slotted guide where only one leaky wave propagates can, when viewed transversely, be represented by a single length of transmission line short-circuited at one end and terminated at the other end in an appropriate lumped network representing the discontinuity.

It has already been mentioned that the only appreciable component of the tangential electric field is the  $z$  component, so that the mode propagating in the slotted waveguide can be regarded as a perturbation on a TE mode propagating in the  $y$  direction (H type mode (i)); besides, " $a$ " and " $b$ " can be chosen such that only the fundamental H type modes are never coupled on such structures<sup>(1)</sup>, so that at the discontinuity the only modes which are excited are H-type modes of all orders, the lowest one being the only one to propagate. Therefore, the waveguide viewed transversely can be represented by a single piece of transmission line of length  $b$ , short circuited at one end and terminated in the appropriate lumped network which will be determined later. In fact, this single transmission line picture is valid only if  $b$  is large enough so that none of the decaying modes can reach the back wall and be reflected with an appreciable amplitude.

$$E_z = E_0 \sin \frac{\pi y}{a} \exp (-jk_z z) \quad (1.1)$$

The  $z$  dependence is the usual  $\exp (-jk_z z)$  dependence and the  $y$  dependence is assumed to be very similar to  $\sin \pi y/a$ , the  $y$  dependence in the closed waveguide.

$E_z$  between the slots, at  $x = b$  is equal to zero. Due to the periodicity of this structure an expansion of  $E_z$  in a Fourier series can be carried out which yields the following expression

$$E_z = \sum_{n=-\infty}^{+\infty} a_n \sin \frac{\pi y}{a} \exp -jk_z z \exp -j(2n\pi z/l) \quad (1.2)$$

If  $\kappa$  is the transverse wave number, corresponding to each  $n$  there will be a  $\kappa_n$  such as

$$\kappa_n^2 = k^2 - (\pi/a)^2 - (k_z + \frac{2n\pi}{l})^2, \quad (1.3)$$

where  $k_z$  is replaced by  $k_z + \frac{2n\pi}{l}$ , according to Eq. (1.2). But  $k_z$  does not differ very much from  $k_{z0}$  for which

$$k^2 = \frac{\pi^2}{a^2} + k_{z0}^2, \quad (1.4)$$

and  $l$  is much smaller than  $\lambda$ ,  $k = 2\pi/\lambda$  is much smaller than  $2\pi/l$ . Therefore, except for  $n = 0$ , which corresponds to the lowest leaky mode,  $\kappa_n$  is approximately equivalent to  $-j(2\pi n/l)$  and the corresponding modes decay rapidly away from the plane  $x = b$ . Even for  $n = 1$  this will be true since  $l$  and  $b$  are of the same order at  $x = -b$  and the fields are too highly attenuated to be appreciably reflected, thus justifying the single transmission line picture. The preceding discussion shows that the electromagnetic energy is partly stored in the neighborhood of the discontinuities, which corresponds to the decaying modes, and partly radiated away.

In the lumped network the radiated energy is represented by a conductance  $G$  and the stored energy by a susceptance  $jB$  as illustrated in Fig. 2.

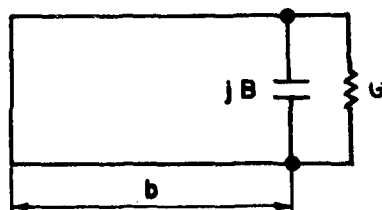


Fig. 2: Transverse equivalent network.

### 1. Determination of G

The conductance  $G$  could be found by computing the power radiated far from the antenna. But the lowest H-type mode ( $n = 0$  in (1.3)), being the only one which is propagating, is the only mode which contributes to the power radiated in the far zone. Therefore, in the determination of  $G$  we can disregard all the space harmonics, and, in so far as  $G$  is concerned, the tangential electric field in the aperture can be taken as

$$E_z = E_0 \sin \frac{\pi Y}{a} \exp -jk_z z \quad (1.5)$$

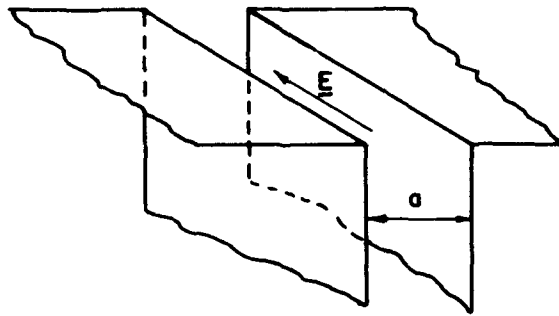


Fig. 3: Parallel plate waveguide radiating into half-space

This corresponds to the situation represented in Fig. 3:  $G$  is the admittance equivalent to a parallel plate waveguide radiating into half space with the electric field parallel to the guide walls. The conductance  $G$  is given by (4)

$$\frac{G}{Y_0} \approx 0.285 \frac{2\pi}{\kappa a} \quad (1.6)$$

where  $Y_0$  is the characteristic admittance of the parallel plate waveguide and the  $\kappa$  the transverse wavenumber given by

$$\kappa^2 = k^2 - k_z^2 - (\pi/z)^2 \quad (1.7)$$

(1.6) can be rewritten

$$\frac{G}{Y_0} = \frac{G_0}{\kappa} 1.6 \text{ where } G_0 = 0.285 \frac{2\pi}{a} \quad (1.8)$$

and  $G_0$  does not depend on  $\kappa$ .

(4) N. Marcuvitz, "Waveguide Handbook", Rad. Lab. Series, Vol. 10, McGraw-Hill Book Co., New York, 1951, p. 191 Eq. 2b.

## 2. Determination of B

The attenuated modes, although not contributing to the power radiated, contribute to the stored energy which is represented in the network by the susceptance  $jB$ . The fields corresponding to these modes have appreciable values only in a fairly limited region which does not extend far from the slots. It is therefore possible to consider that the field distribution depends mostly on the geometry of the slots and very little on the surrounding region. Accordingly, it does not make much difference if we replace the structure represented in Fig. 4. a, (which is the actual structure studied here) by the structure of Fig. 4. b.

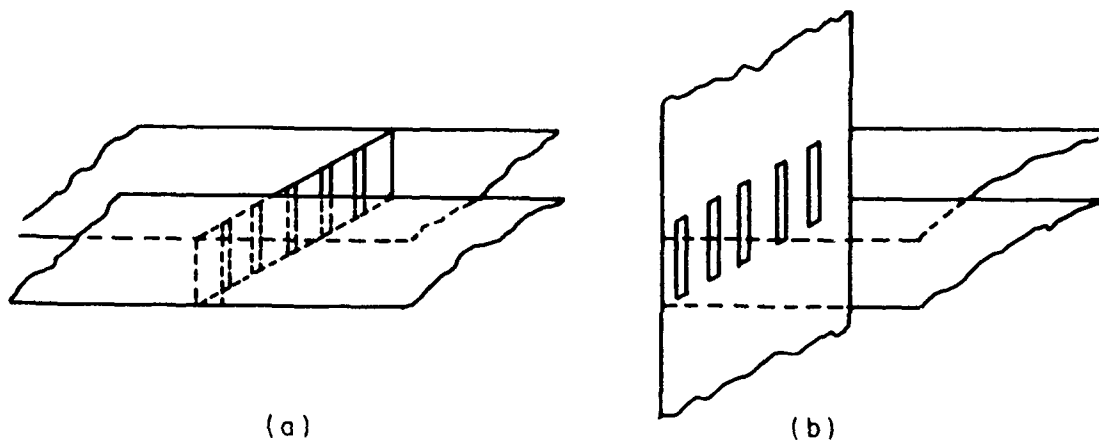


Figure 4: Equivalent Radiating Structures

Clearly this is not completely rigorous since the field distributions corresponding to the decaying modes in the structures illustrated above are likely to differ slightly. However, the results derived from this approximation yield results in excellent agreement with experimental data.

Furthermore the parallel plate waveguide with an array of transverse slots cut in a plane perpendicular to its walls as illustrated in Fig. 4. b has for an image an array of infinite slots cut in an infinite conducting plane. The susceptance of such a discontinuity with tangential magnetic field parallel to the edges of the slots is found to be<sup>(5)</sup>

$$\frac{B}{Y_0} \approx \frac{2\kappa l}{\pi} \ln \csc \frac{\pi d}{2l} \quad (1.9)$$

which can be rewritten

$$\frac{B}{Y_0} = B_0 \kappa \quad (1.9a)$$

(5) N. Marcuvitz, "Waveguide Handbook", Rad. Lab. Series, Vol. 10, McGraw-Hill Book Co., New York, 1951, p. 280 Eq. 1a.

where  $B_0 = \frac{2\ell}{\pi} \ln \csc(\pi d/2\ell)$ , (which does not depend on  $\kappa$ ).

(b) Transverse resonance

The second part in this problem is to determine  $\kappa$  from the network representation by means of a resonance procedure. The resonance equation can be written in the following manner

$$\overleftrightarrow{Y}(\kappa) = \overleftarrow{Y}(\kappa) + \overrightarrow{Y}(\kappa) = 0 \quad (2.10)$$

where  $\overleftarrow{Y}(\kappa)$  is (see Fig. 2) the admittance of the short-circuited piece of transmission line i. e.  $-j Y_0 \cot \kappa b$  and  $\overrightarrow{Y}(\kappa)$  the net admittance of the lumped network representing the discontinuities i. e.  $G + jB$ . Therefore (2.10) becomes

$$-j Y_0 \cot \kappa b + jB + G = 0 \quad (2.11)$$

or

$$-j \cot \kappa b + jB_0 \kappa + \frac{G_0}{\kappa} = 0 \quad (2.12)$$

thus,

$$\cot \kappa b = B_0 \kappa - j \frac{G_0}{\kappa}, \quad (2.13)$$

and dividing both sides by  $\kappa b$ , we see that

$$\frac{\cot \kappa b}{\kappa b} = \frac{B_0}{b} - j \frac{G_0}{\kappa^2 b} \quad (2.14)$$

Let  $xb = u$ , Eq. 2.14 becomes

$$\frac{\cot u b}{u} = \frac{B_0}{b} - j \frac{G_0 b}{u^2} \quad (2.15)$$

This resonance equation should be identical to the equation obtained by Hyneman<sup>(6)</sup> in which he started from the field equations. But whereas the left-hand sides are identical, the right-hand side is here in a simple compact form as opposed to Hyneman's which uses a product of complicated series and integrals. However, once these integrals and series are evaluated the results should be the same, since in the Waveguide Handbook the discontinuities were evaluated from the field equations. One of the principal advantages of the approach used here is that it does not carry out these complicated computations and uses results already available.

---

(6) See Ref. no. (3) Eq. 14 p. 337.

### 1. Leaky-wave solutions

It is clear from Eq. 2.14 that the solution for  $\kappa$  has to be complex, corresponding to a leaky-wave solution. Since the slots are small (Sec. 1a) the solution  $\kappa$  of 2.14 can be regarded as a perturbation on the dominant  $H_{10}$  mode in a completely closed waveguide for which there is no  $x$  dependence, and therefore  $\kappa = 0$ . Thus, it is expected that the resonant value of  $\kappa$  and accordingly of  $u$  will be small. So, in order to find the value of  $\kappa$  for the lowest leaky-wave on the structure, the left hand side of Equation (2.15) can be expanded in powers of  $u = \kappa b$ , keeping only the first two terms and neglecting terms of higher order.

$$\cot u = \frac{\cos u}{\sin u} \approx \frac{1 - \frac{u^2}{2}}{u - \frac{u^3}{6}} \approx \frac{1}{u} \left(1 - \frac{u^2}{2} + \frac{u^2}{6}\right) = \frac{1}{u} - \frac{u}{3}$$

so (7)

$$\frac{\cot u}{u} \approx \frac{1}{u^2} - \frac{1}{3} \quad (2.16)$$

Substituting in (2.15), we get

$$\frac{1}{u^2} - \frac{1}{3} = \frac{B_0}{b} - j \frac{G_0 b}{u^2} \quad (2.17)$$

or

$$1 - \frac{u^2}{3} = \frac{B_0}{b} u^2 - j G_0 b \quad (2.18)$$

Using  $\kappa = u/b$

$$\kappa^2 = \frac{1}{b^2} \frac{1 + j G_0 b}{\frac{B_0}{b} + \frac{1}{3}} \quad (2.20)$$

So  $\kappa$  can be calculated, taking the square root of  $\kappa^2$  with positive real and imaginary part which indicates the leaky-wave behavior. From  $\kappa$ ,  $k_z$  can be found as

$$k_z = \beta - j\alpha = \sqrt{k^2 - \left(\frac{\pi}{a}\right)^2 - \kappa^2} \quad (2.21)$$

where  $\alpha$  is the attenuation constant per unit length and  $\beta$  the phase shift per unit

---

(7) The first term neglected in the expansion of  $(\cot u/u)$  is  $(-u^2/45)$ . Since in most cases of interest  $|u|$  turns out to be close to 1 this approximation is generally better than 5% accurate.

length (in the  $z$ -direction). Dividing both sides of (2.21) by  $k = 2\pi/\lambda$  yields

$$\frac{\lambda}{\lambda_g} - j \frac{\alpha \lambda}{2\pi} = \sqrt{1 - (\lambda/2a)^2 - (\kappa \lambda / 2\pi)^2} \quad (2.22)$$

$\lambda_g$  is the guide wavelength  $\lambda_g = 2\pi/\beta$ . Therefore

$$\frac{\lambda}{\lambda_g} = \text{Re} \sqrt{1 - (\lambda/2a)^2 - (\kappa \lambda / 2\pi)^2} \quad (2.23)$$

and

$$\alpha \lambda = -2\pi \text{Im} \sqrt{1 - (\lambda/2a)^2 - (\kappa \lambda / 2\pi)^2} \quad (2.24)$$

In cases considered here where  $|\kappa|$  is small, a more explicit functional dependence can be obtained by means of a perturbation method. Let  $k_{z0}$  be the longitudinal wavenumber for the closed waveguide

$$k_{z0} = \sqrt{k^2 - (\pi/a)^2}, \quad (2.25)$$

and (2.21) can be rewritten

$$k_z = \beta - j\alpha = \sqrt{k_{z0}^2 - \kappa^2} \quad (2.26)$$

$$\frac{k_z}{k_{z0}} = \sqrt{1 - (\kappa/k_{z0})^2} \quad (2.27)$$

which can be expanded in a power series of  $\kappa^2/k_{z0}^2$  which is, neglecting terms of higher order than  $\kappa^2/k_{z0}^2$

$$\frac{k_z}{k_{z0}} \sim 1 - \frac{\kappa^2}{2k_{z0}^2} \quad (2.28)$$

Hence

$$k_z \approx k_{z0} - \frac{\kappa^2}{2k_{z0}} \quad (2.28a)$$

Substituting for  $\kappa^2$  the value given by Eq. (2.20)

$$k_z \approx k_{z0} - \frac{1}{2b^2 k_{z0}} \frac{1 + jG_0 b}{\frac{B_0}{b} + \frac{1}{3}} \quad (2.29)$$

from which  $\alpha$  is evaluated as

$$\alpha = \frac{1}{2 b k_{z0}} \frac{G_0}{\frac{B_0}{b} + \frac{1}{3}} ; \quad (2.30)$$

then

$$\alpha \lambda = \frac{\lambda}{2 b k_{z0}} \frac{G_0}{\frac{B_0}{b} + \frac{1}{3}} \quad (2.31)$$

or

$$\alpha \lambda = \frac{\lambda \lambda_{g0}}{4 \pi b} \frac{G_0}{\frac{B_0}{b} + \frac{1}{3}} \quad (2.31a)$$

where  $\lambda_{g0}$  is the closed guide wavelength. Similarly for  $\beta$ ,

$$\beta = k_{z0} - \frac{1}{2 b^2 k_{z0}} \frac{1}{\frac{1}{3} + \frac{B_0}{b}} \quad (2.32)$$

or

$$\frac{\lambda}{\lambda_g} = \frac{\lambda}{\lambda_{g0}} - \frac{\lambda \lambda_{g0}}{8 \pi^2 b^2} \frac{1}{\frac{1}{3} + \frac{B_0}{b}} \quad (2.32a)$$

## 2. Surface wave solution

It is clear that Equation (2.14)

$$\frac{\cot \kappa b}{\kappa b} = \frac{B_0}{b} - j \frac{G_0}{\kappa^2 b} \quad (2.14)$$

does not admit any real or purely imaginary solution for  $\kappa$ . Therefore, in so far as the network representation derived in Sec. IIa is valid, there cannot be at the same time a leaky-wave and a surface wave supported by the structure considered here. This is in contradiction with what Hyneman<sup>(8)</sup> seemed to have observed.

Moreover if a surface wave was to be excited alone there would be no power radiated at infinity and the term in  $G$  of Eq. 2.14 would vanish. Eq. (2.14) would reduce to

$$\frac{\cot \kappa b}{\kappa b} = \frac{B_0}{b} \quad (2.33)$$

---

(8) See Reference no. (3) Sec. D., pp. 339, 340.

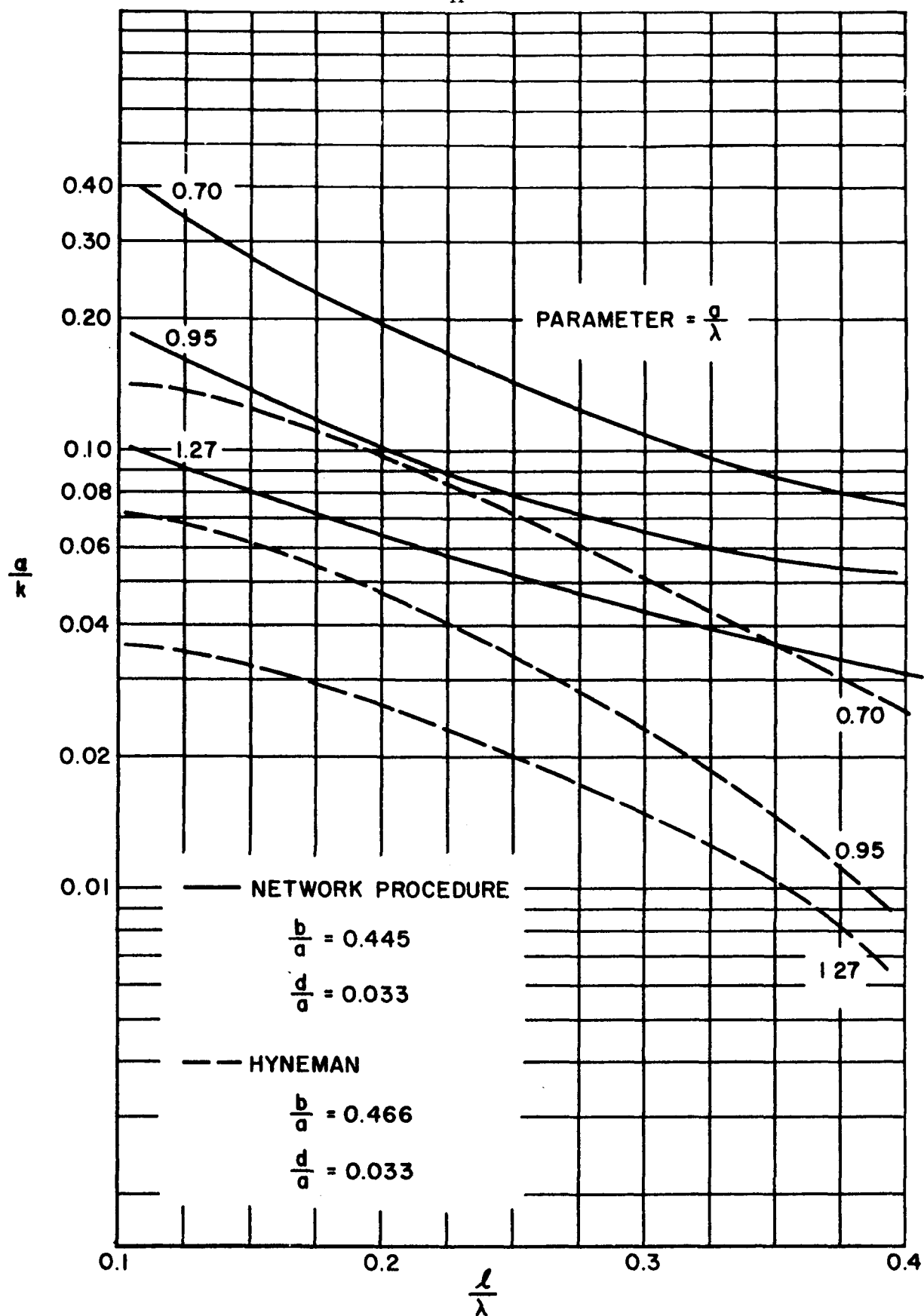


Fig.5. THEORETICAL ATTENUATION vs.  
SLOT SPACING IN WAVELENGTHS

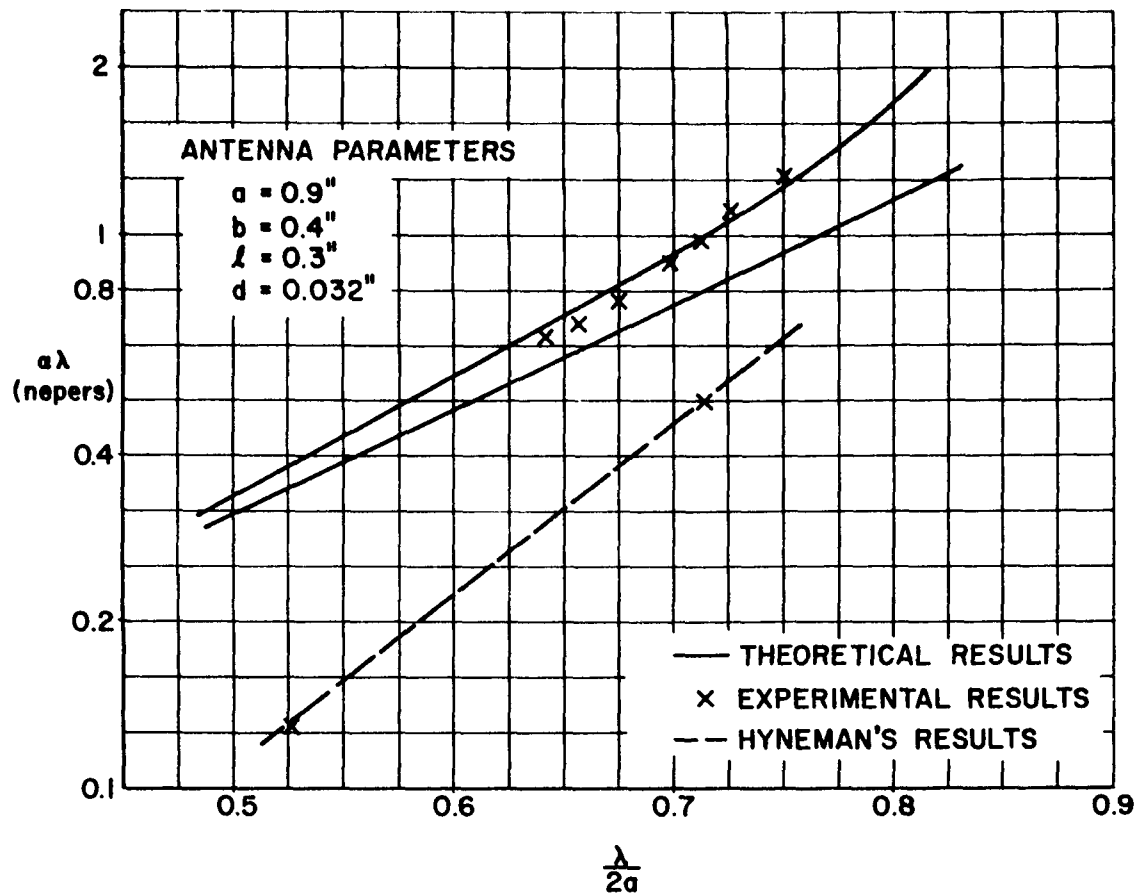
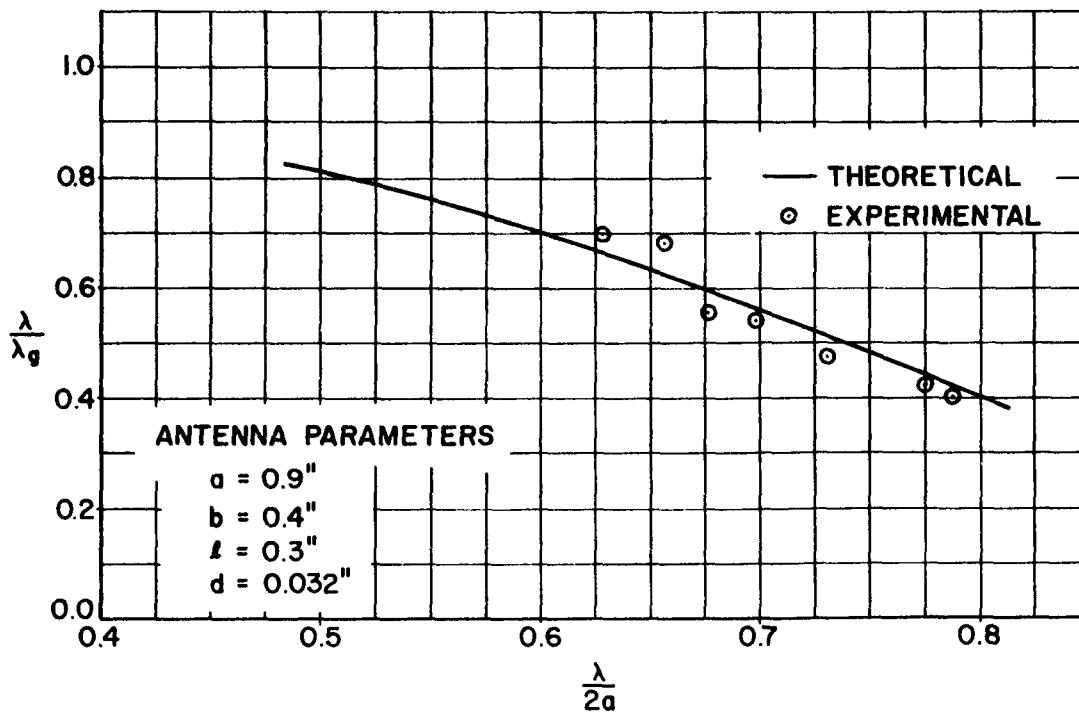


Fig. 6. ATTENUATION vs. WAVELENGTH

Fig. 7.  $\frac{\lambda}{\lambda_g}$  vs. WAVELENGTH

### III. RESULTS

#### a. Theoretical Results

From the expression (2.24) the normalized attenuation constant  $\alpha/k = \alpha\lambda/2\pi$  was computed. The results are plotted on Fig. 5 for several values of  $\alpha/\lambda$ , versus the spacing of the slots  $l/\lambda$ . On the same figure are compared the results obtained by Hyneman for a waveguide only slightly different: the obviously disagree.

On Fig. 6 the plots of attenuation constants  $\alpha\lambda$  versus  $\lambda/2a$  are found first as computed from Eq. (2.24) and then from the perturbational expression as in (2.31) (2.31). The discrepancy between these two curves, though increasing with the wavelength, is always relatively small. In fact, whereas neglecting  $u^2/45$  in the expansion of  $\cot u/u$  is an excellent approximation since  $|u|$  is found to be close to 1, it is not such a good approximation to neglect terms of the order  $\kappa^4/(8k_{z0}^3)$  in the expansion of  $k_z$  in (2.27) because for  $b = 0.4''$ ,  $|\kappa| = |u|/b$  is equivalent to  $|\kappa| \approx 2.5$ .

In any case, the perturbation expression is a far better approximation than Hyneman's results<sup>(8)</sup> which are plotted on the same figure and show clearly the functional dependence of the leaky-wave characteristics.

Finally on Figure 7  $\lambda/(\lambda_g)$  versus  $\lambda/2a$  is plotted as given by Eq. (2.23).

#### b. Experimental Results

An antenna of the type described in the introduction of this report was constructed as illustrated in Fig. 8.

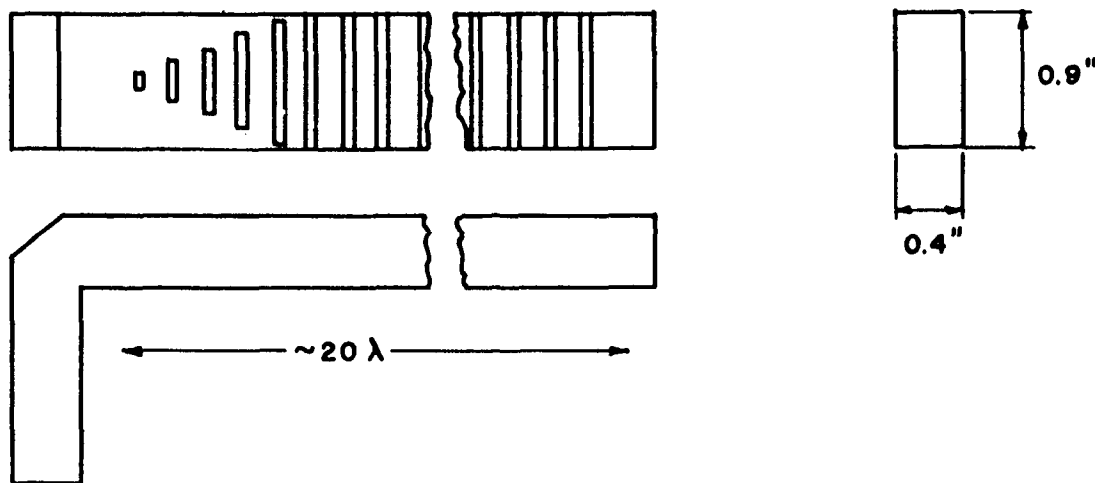


Fig. 8 Antenna constructed for the measurements.

(8) There were only two points available in Hyneman's report (Ref. (3)) to plot the curve of Fig. 6.

In order to avoid reflections at the open end of the guide, the length of the antenna was taken to be around 20 wavelengths so that no wave reach the end with an appreciable amplitude. In addition, it was found necessary to increase progressively the length of the slots, because if they all extended completely across the broad face, the discontinuity in the neighborhood of the first ones could be important enough to excite a strong space-wave which would almost conceal completely the leaky wave.

The waveguide was inserted in a large aluminum ground plane 8' X 8' and radiated into a microwave darkroom approximately 10' X 10' X 10' the walls of which were covered with an absorbing material. The probe consists of a length of flexible miniature coaxial cable which is supported by a polyfoam structure and is covered by absorbing material to minimize as much as possible the distortion of the field. The probe carriage is motor driven and its travel is controlled by limit switches and a reversing switch.

#### 1. Attenuation measurements.

The probe is oriented perpendicularly to the slotted face of the antenna. The signal available from the probe is fed to a recorder through a DC amplifier (Fig. 9). As the probe travels along the antenna at a uniform speed, the recorder plots the amplitude distribution of the leaky wave. These data are plotted on semi-log graph paper, the slope of the straight line which best fits a particular set of data is used to compute the attenuation constant. The results so obtained are shown on Fig. 6.

#### 2. Phase measurements.

The phase measurements are taken with the configuration slightly modified. A null method is used to compare the phases of the aperture field and of a reference signal. The magnitude and phase of this reference are adjusted by means of a calibrated attenuator and a slotted section. Comparison of the phases is accomplished by a hybrid tee junction. A block diagram of the set up used here is shown in Fig. 10. The experimental values of the guide wavelength are plotted on Fig. 7.

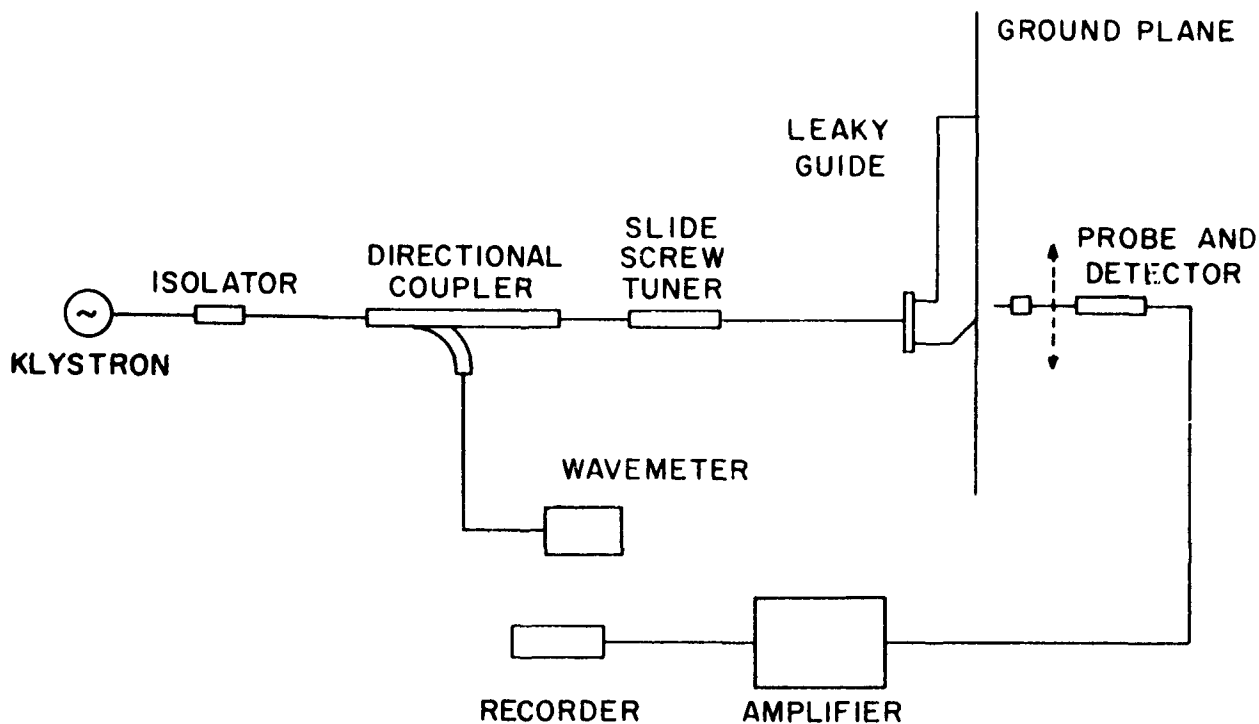


Fig. 9 Block diagram of equipment for attenuation measurement.

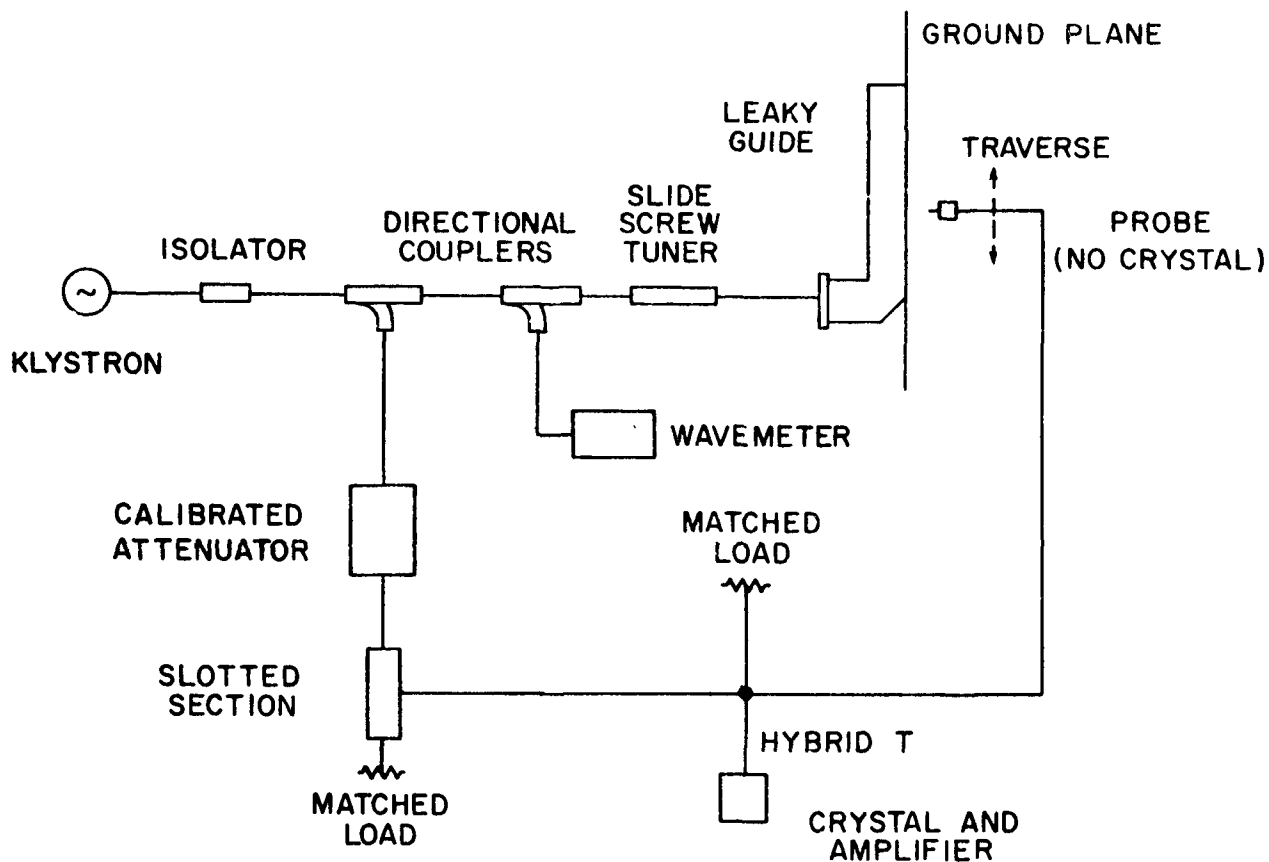


Fig. 10 Block diagram of equipment for guide wavelength measurement.

#### IV. CONCLUSIONS

The experimental results obtained for the attenuation constant and the guide wavelength agree very satisfactorily with the theoretical values (see Fig. 6 and 7). This fact shows that those approximations which were made in Section IIa were perfectly justified.

The validity of the network representation used here seems therefore to be fully guaranteed, and the results derived therefrom are in far better agreement with measured values than any results previously derived by other methods.

Furthermore, it becomes very doubtful that this structure could excite a surface wave together with a leaky wave, as indicated by Hyneman.

# Distribution List

<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>
AFGC (PGAPI) Eglin, AFB, Fla.	1	ASD (ASRNRE-3) Attn: Mr. P. Springer Wright-Patterson AFB, Ohio	1
RADC (RAALD) Attn: Documents Library Griffiss AFB, N. Y.	1	Foreign Technology Division (TDEE) Wright-Patterson AFB, Ohio	1
RADC (RCE) Attn: Dr. John S. Burgess Griffiss AFB, N. Y.	1	WADD (SWDRTR, Mr. A. D. Clark) Directorate of System Engineering Dyna Soar Engineering Office Wright-Patterson AFB, Ohio	1
AF Missile Dev. Cent. (MDGRT) Holloman AFB, New Mexico	1	Lt. Col. Jensen (SSTRE) Space Systems Division Air Force Unit Post Office Los Angeles 45, Calif.	1
Director of Resident Training 3380th Technical Training Group Keesler AFB, Mississippi Attn: OA-3011 Course	1	Director Evans Signal Laboratory Belmar, New Jersey Attn: Mr. O. C. Woodyard	1
SAC (Operations Analysis Office) Offutt AFB, Nebraska	1	Commanding General USASRDL Ft. Monmouth, N. J. Attn: Tech. Doc. Ctr. SIGRA/ SL-ADT	1
AUL Maxwell AFB, Alabama	1	Department of the Army Office of the Chief Signal Officer Washington 25, D. C. Attn: ISGRD-4a-2	1
AF Missile Test Center Partick AFB, Fla. Attn: AFMTC, Tech Library MU-135	1	Massachusetts Institute of Technology Signal Corps Liaison Officer Cambridge 39, Mass Attn: A. D. Bedrosian Rm. 26-131	1
USAF Security Service (CLR) San Antonio, Texas	1	Commanding General USASRDL Ft. Monmouth, N. J. Attn: Mr. F. J. Triola	1
OAR (RROS, Col. J. R. Fowler) Tempo D 4th and Independence Avenue Washington 25, D. C.	1	Commanding General USAMC Attn: AMCRD-RS-PE-E Washington 25, D. C.	1
Hq. USAF (AFOAC-S/ E) Communications-Electronics Directorate Washington 25, D. C.	1	Director U. S. Army Ordnance Ballistic Research Laboratories Aberdeen Proving Ground, Md. Attn: Ballistic Measurements Laboratory	1
AFOSR, OAR (SRYP) Tempo D 4th and Independence Avenue Washington 25, D. C.	1		
Hq. OAR (RROSP, Maj. R. W. Nelson) Tempo D 4th and Independence Washington 25, D. C.	1		
ASD (ASNRR) Wright-Patterson AFB, Ohio	1		
ASD (ASRNC, Mr. W. J. Portune) Wright-Patterson AFB, Ohio	1		

Distribution List (continued)

<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>
Ballistic Research Laboratories Aberdeen Proving Ground, Md. Attn: Tech. Info. Branch	1	Director National Security Agency Ft. G.G. Meade, Maryland Attn: C3/CDL	1
Guided Missile Fuze Library Diamond Ordnance Fuze Labs. Washington 25, D.C. Attn: R.D. Hatcher, Chief Microwave Dev. Section	1	National Aeronautical Space Agency Langley Aeronautical Research Lbs. Langley, Va. Attn: Mr. Cliff Nelson	1
Commanding General USASRDL Fort Monmouth, N.J. Attn: SIGFM/EL-AT	1	OFCRL, OAR (CRXRA-Stop 39) L.G. Hanscom Field, Bedford, Mass (to be shipped under separate cover as reports go to our documents section)	10
Redstone Scientific Info. Center U.S. Army Missile Command Redstone Arsenal, Ala.	5	AFCRL, Office of Aerospace Research (CRD) Attn: Contract Files L.G. Hanscom Field, Bedford, Mass.	2
Commanding General, SIGFM/EL-PC USASRDL Ft. Monmouth, N.J. Attn: Dr. H.H. Kedesdy Deputy Chief, Chem-Physics Branch	1	AFCRL, Office of Aerospace Research (CRD) Attn: Crylyle J. Sletten L.G. Hanscom Field Bedford, Mass.	3
Defense Documentation Center (DDC) Cameron Station Alexandria, Va.	10	Hq. ESD (ESRDW, Maj. J.J. Hobson L.G. Hanscom Field, Bedford, Mass.	1
Library National Bureau of Standards Boulder Laboratories Boulder, Colorado	2	Electronic Systems Division (AFSC) Technical Info. Services Division (ESAT) L.G. Hanscom Field Bedford, Mass.	1
Defense Research Member Canadian Joint Staff 2450 Massachusetts Ave., N.W. Washington 8, D.C.	1	Hq. AFCRL, OAR (CRXR, J.R. Marple) L.G. Hanscom Field, Bedford, Mass.	1
Scientific and Technical Info. Facility Attn: NASA Representative (S-AK/DL) Post Office Box 4700 Bethesda, Md.	1	Chief, Bureau of Ships Department of the Navy Washington 25, D.C. Attn: Code 690	1
National Bureau of Standards U.S. Department of Commerce Washington 25, D.C. Attn: G. Shapiro (Chief, Eng. Elec. Sec. Electricity and Electronics Division)	1	Chief, Bureau of Naval Weapons Department of the Navy Washington 25, D.C. Attn: DLI-31	2
Office of Scientific Intelligence Central Intelligence Agency 2430 E. Street, N.W. Washington 25, D.C.	1		

Distribution List (continued)

<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>
Commander U.S. Naval Air Missile Test Center Point Mugu, Calif. Attn: Code 366	1	Commanding Officer and Director U.S. Navy Electronics Laboratory (Library) San Diego 52, Calif.	1
U.S. Naval Ordnance Labs. White Oak Silver Spring 19, Md. Attn: The Library	1	Commander U.S. Naval Air Test Center Patuxent River, Md. Attn: ET-315, Antenna Branch	1
Commander U.S. Naval Ordnance Test Station China Lake, Calif. Attn: Code 753	1	Material Laboratory, Code 932 New York Naval Shipyard Brooklyn 1, New York Attn: Mr. D. First	1
Librarian U.S. Naval Postgraduate School Monterey, Calif.	1	Chief, Bureau of Ships Department of the Navy Washington 25, D.C. Attn: Code 817B	1
National Aeronautics and Space Administration Attn: Antenna Systems Branch Goddard Space Flight Center Greenbelt, Md.	1	AFSC STLO (RTSNW) c/o Dept of the Navy Room 3710 Main Navy Bldg. Washington 25, D.C.	1
Director U.S. Naval Research Labs. Washington 25, D.C. Attn: Code 2027	2	Aero Geo Astro Corp. 1200 Duke Street Alexandria, Va. Attn: Library	1
Dr. J.I. Bohnert Code 5210 U.S. Naval Research Laboratory Washington 25, D.C.	1	Aerospace Corp. Box 95085 Los Angeles 45, Calif. Attn: Library	1
Commanding Officer and Director U.S. Navy Underwater Sound Laboratory Fort Trumbull, New London Connecticut	1	Airborne Instruments Laboratory, Inc. Division of Cutler Hammer Walt Whitman Road Melville, New York Attn: Library	1
Chief of Naval Research Department of the Navy Washington 25, D.C. Attn: Code 427	1	Aircom, Inc. 48 Cummington Street Boston, Mass.	1
Commanding Officer U.S. Naval Air Development Center Johnsville, Penn. Attn: NADC Library	1	Andrew Alford Consulting Engineers 299 Atlantic Avenue Boston 10, Mass	1
Office of Naval Research Branch Office, London Navy 100, Box 39 F.P.O. N.Y., N.Y.	10	Aerospace Corp. Satellite Control Attn: Mr. R.C. Hansen P.O. Box 95085 Los Angeles 45, Calif.	1

Distribution List (continued)

<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>
ACF Electronics Div. Electro-Physics Labs. Attn: Library 3355 52nd Avenue Hyattsville, Md.	1	Brush Beryllium Company 17876 St. Clair Street Cleveland 10, Ohio Attn: N.W. Bass	1
Battelle Memorial Institute 505 King Avenue Columbus 1, Ohio Attn: Wayne E. Rife, Project Leader Electrical Engr. Division	1	Chance Vought Corp. 9314 W. Jefferson Blvd. Dallas, Texas Attn: A.D. Pattullo, Librarian	1
Bell Aircraft Corp. P.O. Box 1 Buffalo 5, N.Y. Attn: E.P. Hazelton, Librarian	1	Chance Vought Corp. Vought Electronics Division P.O. Box 5907 Dallas 22, Texas	1
Bell Telephone Labs. Murray Hill, N.J.	1	Chu Associates P.O. Box 387 Whitcomb Avenue Littleton, Mass.	1
Bell Telephone Labs, Inc. Technical Information Library Whippany Laboratory Whippany, N.J. Attn: Technical Reports Librarian	1	Collins Radio Co. 855 35th Street, N.W. Cedar Rapids, Iowa Attn: Dr. R.L. McCraery	1
Bendix Pacific Division 11600 Sherman Way North Hollywood, Calif. Attn: Engr. Library	1	Cornell Aeronautical Laboratory Inc. 4455 Genesee Street Buffalo 21, New York Attn: Librarian	1
Bendix Radio Division Bendix Aviation Corp. E. Joppa Road Towson 4, Md. Attn: Dr. D.M. Allison, Jr. Director, Engr. and Research	1	Dalmo Victor Company A Division of Textron, Inc. 1515 Industrial Way Belmont, Calif. Attn: M.E. Addams, Technical Librarian	1
Bjorksten Research Labs, Inc. P.O. Box 265 Madison, Wis. Attn: Librarian	1	Dorne and Margolin, Inc. 29 New York Avenue Westbury, L.I., N.Y.	1
Boeing Airplane Co. Pilotless Aircraft Division P.O. Box 3707 Seattle 24, Washington Attn: R.R. Barber Library Supervisor	2	Aircraft Division Douglas Aircraft Co., Inc. 3855 Lakewood Blvd. Long Beach, Calif. Attn: Technical Library	1
Boeing Company 3801 3801 S. Oliver Street Wichita 1, Kansas Attn: K.C. Knight, Library Supervisor	1	Douglas Aircraft Co., Inc. 3000 Ocean Park Blvd. Santa Monica, Calif. Attn: P. Duyan, Jr. Chief, Electrical/ Electronics Section	1

# Distribution List (continued)

<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>
Douglas Aircraft Co., Inc. 2000 North Memorial Drive Tulsa, Oklahoma Attn: Engr. Librarian, D-250	1	ITT Federal Laboratories Technical Library 500 Washington Avenue Nutley 10, N. J.	1
Electromagnetic Research Corp. 5001 College Avenue College Park, Md. Attn: Mr. M. Katzin	1	Gabriel Electronics Division Main and Pleasant Streets Millis, Mass. Attn: Dr. Edward Altshuler	1
Electronics Communication 1830 York Road Timonium, Md.	1	General Electric Company Building 3 - Rm 143-1 Electronics Park Syracuse, N. Y. Attn: Y. Burke Documents Library	1
Convair, A Division of General Dynamics Corp. Fort Worth, Texas Attn: K.G. Brown Division Research Librarian	1	General Electric Co. Missile and Space Vehicle Dept. 3198 Chestnut Street Philadelphia, Pa. Attn: Documents Library	1
Convair, A Division of General Dynamics Corp. 3165 Pacific Highway San Diego 12, Calif. Attn: Mrs. Dora Burke Engr. Librarian	1	General Electric Company 3750 D Street Philadelphia 24, Pa. Attn: Mr. H.G. Lew Missile and Space Vehicle Dept.	1
Electronic Speciality Co., 5121 San Fernando Road Los Angeles 39, Calif. Attn: D.L. Margerum Chief Engineer, Radiating Systems Division	1	General Precision Laboratory, Inc. 63 Bedford Road Pleasantville, N. Y. Attn: Librarian	1
Emerson and Cuming, Inc. 59 Walpole Street Canton, Mass. Attn: Mr. W. Cuming	1	Goodyear Aircraft Corp. 1210 Massillon Road Akron 15, Ohio Attn: Library, Plant G	1
Emerson Electric Mfg. Co. 8100 W. Florissant Avenue St. Louis 21, Miss. Attn: Mr. E.R. Breslin, Librarian	1	Granger Associates Electronic Systems 974 Commerical Street Palo Alto, Calif. Attn: J.V.N. Granger, President	1
Emerson Radio-Phonograph Corp. Emerson Research Laboratories 1140 Eastwest Highway Silver Spring, Maryland Attn: Mrs. R. Corbin, Librarian	1	Grumman Aircraft Engr. Corp. Bethpage, L.I., N. Y. Attn: Engr. Librarian Plant No. 5	1
Fairchild Stratos Corp. Hagerstown, Md. Aircraft Missiles Division Attn: Library	1	Hallicrafters Co. 4401 W. 5th Avenue Chicago 24, Ill. Attn: L. LaGioia, Librarian	1

Distribution List (continued)

<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>
The Hallicrafters Co. 5th and Kostner Avenues Chicago 24, Ill. Attn: H. Hodara Head of Space Communication	1	Dr. Henry Jasik, Consulting Engineer 298 Shames Drive Brush Hollow Industrial Park Westbury, N. Y.	1
Hoffman Electronics Corp. 3761 South Hill Street Los Angeles 7, Calif. Attn: Engineering Library	1	Lockheed Aircraft Corp. 2555 N. Hollywood Way California Division Engineering Labs. Department 72-25 Plant A-1, Bldg. 62-1 Burbank Calif. Attn: N.C. Harnois	1
Hughes Aircraft Co. Antenna Department Building 12, Mail Station 2714 Culver City, Calif. Attn: Dr. W.H. Kummer	1	Lockheed Aircraft Corp. Missiles and Space Division Technical Information Center 2351 Hanover Street Palo Alto, Calif.	2
Sperry-Rand Research Center Route 117 (North Road) Sudbury, Mass Attn: Mr. G. Meltz	1	Martin-Marietta Corp. 12250 S. State Highway 65 Jefferson County, Colo. Attn: Mr. J. McCormick	1
Hughes Aircraft Company Florence Avenue and Teale Streets Culver City, Calif. Attn: L. L. Balin Manager, Antenna Dept.	1	The Martin Co. Baltimore 3, Md. Attn: Engr. Library Antenna Design Group	1
Hughes Aircraft Co. Attn: Mr. L. Stark, Microwave Dept. Radar Laboratory, P.O. Box 2097 Building 600, Mail Station C-152 Fullerton, Calif.	1	Mathematical Reviews 190 Hope Street Providence 8, R.I.	1
International Business Machines Corp. Space Guidance Center Federal Systems Division Owego, Tioga County, N.Y. Attn: Technical Reports Center	1	The W. L. Maxson Corp. 475 10th Avenue New York, N. Y. Attn: Miss D. Clark	1
International Resistance Co. 401 N. Broad Street Philadelphia 8, Pa. Attn: Research Library	1	Mc Donnell Aircraft Corp. Dept. 644 Box 615 St. Louis 66, Mo. Attn: C.E. Zollar Engineering Library	1
ITT Federal Laboratories 3700 E. Pontiac Street Fort Wayne 1, Indiana Attn: Technical Library	1	Mc Millan Laboratory Inc. Brownville Avenue Ipswich, Mass. Attn: Security Officer Document Room	1
Atlantic Research Corp. Shirley Highway at Edsall Rd. Alexandria, Va. Attn: D.C. Ports	1	Melpar, Inc. 3000 Arlington Blvd. Falls Church, Va. Attn: Engr. Technical Library	1
		Microwave Associates, Inc. South Avenue Brulington, Mass.	1

# Distribution List (continued)

<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>	<u>No.</u>	<u>Copies</u>
Microwave Development Labs. Inc. 92 Broad Street Wellesley 67, Mass. Attn: N. Tucker, General Manager	1	Philco Corp. Research Division Union Meeting Pond Blue Bell, Pa. Attn: Research Librarian	1	
The Mitre Corp. 244 Wood Street Lexington 73, Mass. Attn: Mrs. Jean E. Claflin Librarian	1	Pickard and Burns, Inc. 103 Fourth Avenue Waltham 54, Mass. Attn: Dr. R.H. Woodward	1	
Motorola, Inc. 8201 E. McDowell Rd. Phoenix Arizona Attn: Dr. T.E. Tice	1	Polytechnic Research and Development Co., Inc. 202 Tillary Street Brooklyn 1, New York Attn: Technical Library	1	
Motorola, Inc. Phoenix Research Laboratory 2102 N. 56 Street Phoenix, Arizona Attn: Dr. A.L. Aden	1	Radiation, Inc. Melbourne, Florida Attn: R.F. Systems Division Technical Info. Center	1	
National Research Council Radio and Electrical Engineering Division Ottawa, Ontario, Canada Attn: Dr. G.A. Miller, Head Microwave Section	1	Radiation Systems, Inc. 440 Swann Avenue Alexandria, Va. Attn: Library	1	
North American Aviation, Inc. 12214 Lakewood Blvd. Downey, Calif. Attn: Technical Info. Center (495-12) Space and Info. Systems Division	1	RCA Laboratories David Sarnoff Research Center 201 Washington Road Princeton, N.J. Attn: Miss F. Cloak, Librarian	1	
North American Aviation, Inc. Los Angeles International Airport Los Angeles 45, Calif. Attn: Engr. Tech. File	1	RCA Defense Electronic Products Building 10, Floor 7 Camden 2, N.J. Attn: Mr. Harold J. Schrader Staff Engineer Organization of Chief Technical Administrator	1	
Page Communications Engrs. Inc. 2001 Wisconsin Avenue, N.W. Washington 7, D.C. Attn: R. Temple, Librarian	1	RCA Missile Control and Electronics Division Bedford Street Burlington, Mass. Attn: Librarian	1	
Northrop Corporation Norair Division 1001 E. Broadway Hawthorne, Calif. Attn: Technical Info. 3924-31	1	RCA Surface Communications Systems Lab. 75 Varick Street New York 13, N.Y. Attn: Mr. S. Krevsky	1	

Distribution List (continued)

<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>
RCA West Coast Missile and Surface Radar Division Engineering Library, Building 306/2 Attn: L. R. Hund, Librarian 8500 Balboa Blvd. Van Nuys, Calif.	1	Ryan Aeronautical Co. 2701 Harbor Drive Lindbergh Field San Diego 12, Calif. Attn: Library	1
RCA Defense Electronic Products Advanced Military Systems Princeton, N. J. Attn: Mr. David Shore	1	Sage Laboratories, Inc. 3 Huron Drive Natick, Mass.	1
Director, USAF Project RAND Via: AF Liaison Office The Rand Corporation 1700 Main Street Santa Monica, Calif.	1	Sanders Associates, Inc. 95 Canal Street Nashua, New Hampshire Attn: Mr. N. R. Wild	1
The Rand Corporation 1700 Main Street Santa Monica, Calif. Attn: Tech. Library	1	Sandia Corporation P. O. Box 5800 Albuquerque, New Mexico Attn: Records Management and Services Department	1
Rantec Corp. 23999 Ventura Blvd. Calabasas, Calif. Attn: Grace Keener, Office Manager	1	Scanwell Laboratories, Inc. 6601 Scanwell Lane Springfield, Va.	1
Raytheon Company Boston Post Road Wayland, Mass. Attn: Mr. Robert Borts	1	STL Technical Library Document Acquisitions Space Technology Laboratories, Inc. P. O. Box 95001 Los Angeles 45, Calif.	1
Raytheon Company Wayland Laboratory Wayland, Mass. Attn: Miss A. G. Anderson Librarian	1	Sperry Gyroscope Co. Great Neck, L. I., N. Y. Attn: F. W. Turnbull Engineering Librarian	1
Raytheon Company Missile Systems Division Hartwell Road Bedford, Mass Attn: D. H. Archer	1	Stanford Research Institute Documents Center Menlo Park, Calif. Attn: Acquisitions	1
Remington Rand UNIVAC Division of Sperry Rand Corp. P. O. Box 500 Blue Bell, Pa. Attn: Engineering Library	1	Sylvania Electric Products, Inc. 100 First Avenue Waltham 54, Mass. Attn: Charles A. Thornhill, Report Librarian Waltham Laboratories Library	1
Republic Aviation Corporation Farmingdale, L. I., N. Y. Attn: Engineering Library	1	Sylvania Elec. Prod. Inc. Electronic Defense Laboratory P. O. Box 205 Mountain View, Calif. Attn: Library	1
		Sylvania Reconnaissance Systems Lab. Box 188, Mountain View, Calif. Attn: Marvin D. Waldman	1

Distribution List (continued)

<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>
TRG, Inc. 400 Border Street East Boston, Mass Attn: Dr. Alan F. Kay	1	University of Southern Calif. University Park Los Angeles, Calif. Attn: Dr. R. L. Chuan Director, Engineering Center	1
AS Thomas, Inc 355 Providence Highway Westwood, Mass. Attn: A.S. Thomas, President	1	Case Institute of Technology Electrical Engineering Department 10900 Euclid Avenue Cleveland, Ohio Attn: Professor R. Plonsey	1
Texas Instruments, Inc. 6000 Lemmon Avenue Dallas 9, Texas Attn: J.B. Travis Systems Planning Branch	1	Columbia University Department of Electrical Engineering Morningside Heights, N.Y. Attn: Dr. Schlesinger	1
Westinghouse Electric Corp. Electronics Division Friendship Int'l Airport Box 1987 Baltimore 3, Md. Attn: Engineering Library	1	University of Southern Calif Engineering Center University Park Los Angeles 7, Calif. Attn: Z.A. Kaprielian Associate Professor of Electrical Engineering	1
Library Geophysical Institute of the University of Alaska College, Alaska	1	Cornell University School of Electrical Engineering Ithaca, New York Attn: Prof. G.C. Dalman	1
Brown University Department of Electrical Engineering Providence, R.I. Attn: Dr. C.M. Angulo	1	University of Florida Department of Electrical Engineering Gainesville, Fla. Attn: Prof. M.H. Latour, Library	1
California Institute of Technology Jet Propulsion Laboratory 4900 Oak Grove Drive Pasadena, Calif. Attn: Mr. I.E. Newlan	1	Library Georgia Technology Research Institute Engineering Experiment Station 722 Cherry Street, N.W. Atlanta, Georgia Attn: Mrs. J.H. Crosland, Librarian	1
California Institute of Technology 1201 E. California Drive Pasadena, Calif. Attn: Dr. C. Papas	1	Harvard University Technical Reports Collection Gordon McKay Library 303 Pierce Hall Oxford Street Cambridge 38, Mass. Attn: Librarian	1
Space Sciences Laboratory Leuschner Observatory University of California Berkeley 4, Calif. Attn: Dr. S. Silver, Professor of Engineering Science and Director, Space Sciences Laboratory	1	Harvard College Observatory 60 Garden Street Cambridge 39, Mass. Attn: Dr. F.L. Whipple	1
University of California Electronics Research Lab. 332 Cory Hall Berkeley 4, Calif. Attn: J.R. Whinnery	1		

Distribution List (continued)

<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>
University of Illinois Documents Division Library Urbana, Illinois	1	McGill University Department of Electrical Engineering Montreal, Canada Attn: Dr. T. Pavlasek	1
University of Illinois College of Engineering Urbana, Illinois Attn: Dr. P.E. Mayes Department of Electrical Engineering	1	University of Michigan Electronic Defense Group Institute of Science and Technology Ann Arbor, Michigan Attn: J.A. Boyd, Supervisor	1
Harvard University Gordon McKay Laboratory 9 Oxford Street Cambridge 38, Mass. Attn: R.W.P. King, Professor of Applied Physics	1	University of Michigan Office of Research Administration Radiation Laboratory 912 N. Main Street Ann Arbor, Michigan Attn: Mr. R.E. Hiatt	1
Harvard University Gordon McKay Laboratory 9 Oxford Street Cambridge 38, Mass. Attn: Prof. S.R. Seshadri	1	University of Michigan Engineering Research Institute Willow Run Laboratories Willow Run Airport Ypsilanti, Michigan Attn: Librarian	1
The Johns Hopkins University Homewood Campus Baltimore 18, Md. Attn: Dr. D.E. Kerr, Department of Physics	1	University of Minnesota Minneapolis 14, Minnesota Attn: Mr. R.H. Stumm, Library	1
The Johns Hopkins University Applied Physics Laboratory 8521 Georgia Avenue Silver Spring, Md. Attn: Mr. G. L. Seielstad	1	Physical Science Laboratory New Mexico State University University Park, New Mexico Attn: Mr. H.W. Haas	1
University of Kansas Electrical Engineering Department Lawrence, Kansas Attn: Dr. H. Unz	1	New York University Institute of Mathematical Sciences Room 802 25 Waverly Place New York 3, New York Attn: Morris Kline	1
Lowell Technological Institute Research Foundation P.O. Box 709 Lowell, Mass. Attn: Dr. C.R. Mingins	1	Northwestern University Microwave Laboratories Evanston, Illinois Attn: R.E. Beam	1
Massachusetts Institute of Technology Research Laboratory of Electronics Building 36, Room 327 Cambridge 39, Mass. Attn: J.H. Hewitt	1	Antenna Laboratory Department of Electrical Engineering The Ohio State University 2024 Neil Avenue Columbus 10, Ohio Attn: Reports Librarian	1
Massachusetts Institute of Technology Lincoln Laboratory P.O. Box 73 Lexington 73, Mass. Attn: M.A. Granese, Librarian	1	The University of Oklahoma Research Institute Norman, Oklahoma Attn: Prof. C.L. Farrar, Chairman Electrical Engineering	1

Distribution List (continued)

<u>Organization</u>	<u>No. of Copies</u>	<u>Organization</u>	<u>No. of Copies</u>
University of Pennsylvania Institute of Cooperative Research 3400 Walnut Street Philadelphia, Pa. Attn: Electrical Engineering Dept.	1	The University of Texas Defense Research Laboratory Austin, Texas Attn: Claude W. Horton Physics Library	1
Polytechnic Institute of Brooklyn Microwave Research Institute 55 Johnson Street Brooklyn 1, New York Attn: Dr. A.A. Oliner	1	University of Toronto Department of Electrical Engineering Toronto, Canada Attn: Prof. G. Sinclair	1
Polytechnic Institute of Brooklyn Microwave Research Institute 55 Johnson Street Brooklyn 1, New York Attn: Mr. A.E. Laemmel	1	University of Washington Department of Electrical Engineering Seattle 5, Washington Attn: D.K. Reynolds	1
The Pennsylvania State University 223 Electrical Engineering University Park, Pa. Attn: A.H. Waynick, Director, Ionosphere Research Laboratory	1	University of Wisconsin Department of Electrical Engineering Madison, Wisconsin Attn: Dr. Scheibe	1
Purdue University Department of Electrical Engineering Lafayette, Indiana Attn: Dr. Schultz	1		
Library W.W. Hansen Laboratory of Physics Stanford University Stanford, California	1		
Syracuse University Research Institute Collendale Campus Syracuse 10, N.Y. Attn: Dr. C.S. Grove, Jr. Director of Engineering Research	1		
Technical University Cestervoldade 10 G Copenhagen, Denmark Attn: Prof. H.L. Knudsen	1		
University of Tennessee Ferris Hall W. Cumberland Avenue Knoxville 16, Tennessee	1		
The University of Texas Electrical Engineering Research Laboratory P.O. Box 8026 University Station Austin 12, Texas Attn: Mr. J.G. Gerhardt	1		11